

Name: \_\_\_\_\_

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1. We call a partition  $\{P_1, \dots, P_k\}$  of  $[n]$  nice iff  $(j + 1) \notin P_i$  for every  $i \in [k]$  and  $j \in P_i$ .  
Prove that number of nice partitions is equal to  $B(n - 1)$ .

2. How many different 6-digit numbers have sum of their digits at most 47?

3. How many ways to put  $n$  indistinguishable balls into  $k$  different boxes if we have to put at least  $a_i$  balls into the box with number  $i$ .