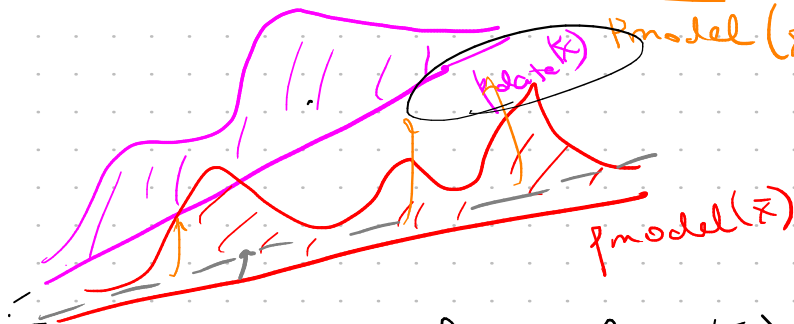


Wasserstein GAN

$$p_{\text{model}}(x) \approx p_{\text{data}}(x)$$

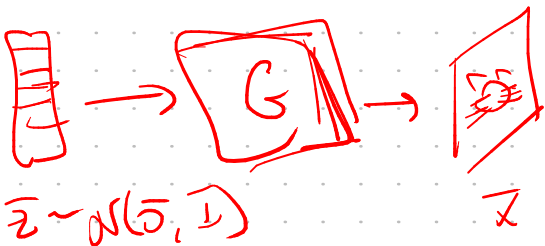
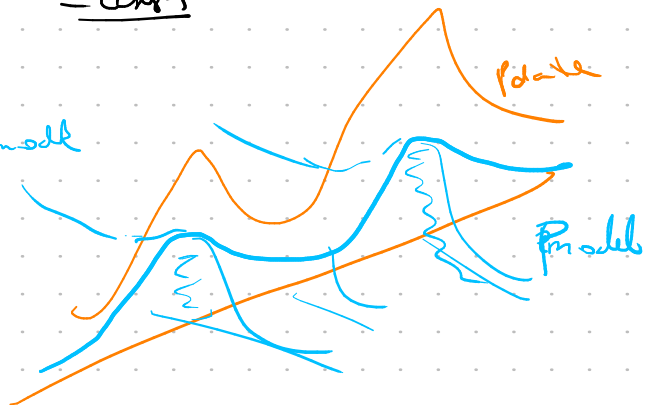
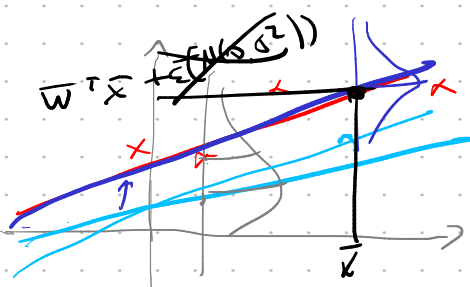
$$KL(p_{\text{data}} || p_{\text{model}}) \rightarrow \min$$

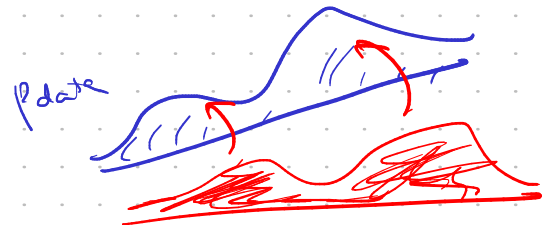


$$KL(p || q) = \int p(x) \log \frac{p(x)}{q(x)} dx = \infty$$

$$KL(q || p) = \infty$$

$$WSD(p || q) = KL(p || \frac{p+q}{2}) + KL(q || \frac{p+q}{2}) = \text{const}$$





Earth Mover Distance EMD
Wasserstein distance

$$W(p, q) = \inf_{\gamma \in \text{Prob}(p \times q)} \int \|\bar{x} - \bar{y}\| d\gamma$$

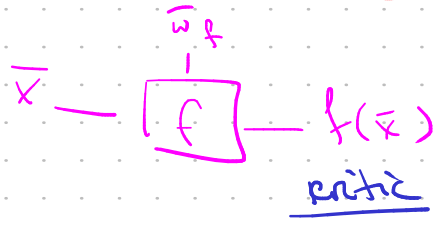
$\int \gamma(\bar{x}, \bar{y}) d\bar{x} = q(\bar{y})$
 $\int \gamma(\bar{x}, \bar{y}) d\bar{y} = p(\bar{x})$



Δ GANs: Noise - Kullback-Leibler
Kantorovich - Rubinstein duality

$$W(p, q) = \sup_{f: \|f\|_{L^1} \leq 1} \left(\mathbb{E}_{p(\bar{x})} [f(\bar{x})] - \mathbb{E}_{q(\bar{x})} [f(\bar{x})] \right)$$

$p_{\text{data}} \quad p_{\text{model}}(\bar{x}) = p_{\theta}(G(\bar{z}))$



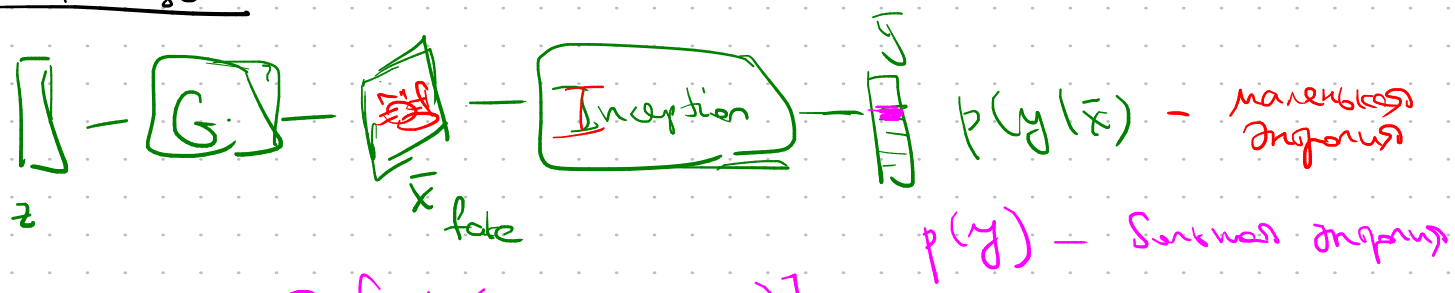
- fix G, θ

$$\mathbb{E}_{\bar{z}} [f] - \mathbb{E}_{G(\bar{z})} [f] \xrightarrow{\bar{w}} \max$$

 - fix \bar{w}, f

$$- \mathbb{E}_{G(\bar{z})} [f] \xrightarrow{\theta} \min$$

Inception score



$$\text{Inception Score} = \mathbb{E}_{\bar{x}} \left[\text{KL}(p(y) \| p(y|\bar{x})) \right]$$

FID - Fréchet Inception Distance

$$d(p_{\text{test}}(G(\bar{z})), p_{\text{test}}(\bar{x}))$$

